

Unequality of mutual actions and powers exchanged between solids S_6 et S_7^k

Mutual actions between both solids

It is interesting to note following both expressions :

$$T\left(S_6 \xrightarrow{C} S_7^k / R_0, A_{7n}^k\right) = A_{7n}^k \begin{pmatrix} \frac{Mg}{8} \cdot \vec{X}_0 \\ 0 \end{pmatrix}$$

and

$$T\left(S_7^k \xrightarrow{C} S_6 / R_0, A_{7n}^k\right) = A_{7n}^k \begin{pmatrix} \frac{rMg}{8R} \cdot \vec{Y}_{1n} \\ 0 \end{pmatrix}$$

The unequality is due to the state of permanent instability of the engine. We notice that vectors action and reaction to contact points A_{7n}^k

- are not equal in module,
- form a variable angle during the rotation.

We have the following unequality: $r < R$, where in points A_{7n}^k .

$$|\vec{F}| \left[S_6 \xrightarrow{C} S_7^k / R_0, A_{7n}^k \right] \gg |\vec{F}| \left[S_7^k \xrightarrow{C} S_6 / R_0, A_{7n}^k \right]$$

The punctual speed of points A_{7n}^k is equal to $\vec{V}_{A_{7n}^k} = R \cdot \Omega \cdot \vec{Y}_{1n}$. In point A_{71}^k , we can write: $\vec{V}_{A_{71}^k} = R \cdot \Omega_{12}^0 \cdot \vec{Y}_{11} = R \cdot \Omega_{12}^0 \left[-\sin(\Omega_{12}^0 \cdot t) \vec{X}_0 + \cos(\Omega_{12}^0 \cdot t) \vec{Y}_0 \right]$.

The instant power exchanged at time t in the point A_{71}^k is then equal to:

$$P_{A_{71}^k} (S_{71}^k \xrightarrow{C} S_6, t) + P_{A_{71}^k} (S_6 \xrightarrow{C} S_{71}^k, t) = \left[\frac{rMg}{8R} \cdot \vec{Y}_{11} + \frac{Mg}{8} \cdot \vec{X}_0 \right] \cdot \vec{V}_{A_{71}^k}$$

$$P_{A_{71}^k} (S_{71}^k \xleftarrow{C} S_6, t) = \Omega_{12}^0 \left[\frac{rMg}{8} - \frac{RMg}{8} \sin(\Omega_{12}^0 t) \right] \neq 0$$

This expression shows that the Newton's 3rd law is violated in the particular point A_{71}^k .

From this formula, we can show that at the instant t of the cycle, the power transmitted in the point A_{71}^k fluctuates around a constant value. The maximum value of the power, when

$\Omega_{12}^0 \cdot t = \frac{3\pi}{2}$, is worth :

$$P_{A_{71}^k} \left(S_{71}^k \xleftarrow{C} S_6, t = \frac{3\pi}{2\Omega_{12}^0} \right) = \Omega_{12}^0 \left[\frac{rMg}{8} + \frac{RMg}{8} \right] > 0$$